

1.  $R^k$ , onde  $k=1, \dots, 4$ , é da forma

$R^k$ : Se  $x_1$  é  $A_1^k$  e  $x_2$  é  $A_2^k$  então  $y$  é  $B^k$

Mamdani:  $\hat{R} = \bigcup_{k=1}^4 \hat{R}^k$ , onde

$$\mu_{\hat{R}^k}(x, y) = \mu_{A^k}(x) \wedge \mu_{B^k}(y) = \mu_{A_1^k}(x_1) \wedge \mu_{A_2^k}(x_2) \wedge \mu_{B^k}(y)$$

Saída fuzzy  $\tilde{B} = \tilde{A} \hat{\vee} \hat{R} = \tilde{A} \hat{\vee} \bigcup_{k=1}^4 \hat{R}^k = \bigcup_{k=1}^4 \tilde{A} \hat{\vee} \hat{R}^k$

Seja  $\tilde{B}^k = \tilde{A} \hat{\vee} \hat{R}^k$  para  $k=1, \dots, 4$

Temos  $\mu_{\tilde{B}^k}(y) = \bigvee_{x \in X} \mu_{\tilde{A}}(x) \wedge \mu_{\hat{R}^k}(x, y)$

$$= \bigvee_{x \in X} \mu_{\tilde{A}}(x) \wedge \mu_{A^k}(x) \wedge \mu_{B^k}(y)$$

$$= \bigvee_{x_1 \in X_1} \bigvee_{x_2 \in X_2} \mu_{\tilde{A}_1}(x_1) \wedge \mu_{\tilde{A}_2}(x_2) \wedge \mu_{A_1^k}(x_1) \wedge \mu_{A_2^k}(x_2) \wedge \mu_{B^k}(y)$$

$$= \left[ \bigvee_{x_1 \in X_1} \mu_{\tilde{A}_1} \wedge A_1^k(x_1) \wedge \bigvee_{x_2 \in X_2} \mu_{\tilde{A}_2} \wedge A_2^k(x_2) \right] \wedge \mu_{B^k}(y)$$

Daí:  $\mu_{\tilde{B}^k}(y) = \left[ \bigvee_{x_1 \in X_1} \mu_{\tilde{A}_1} \wedge A_1^k(x_1) \wedge \bigvee_{x_2 \in X_2} \mu_{\tilde{A}_2} \wedge A_2^k(x_2) \right] \wedge \mu_{B^k}(y)$

$$= [0.5 \wedge 0.5] \wedge \mu_{B^1}(y) = 0.5 \wedge \mu_P(y)$$

$$\mu_{\tilde{B}^2}(y) = [0.5 \wedge 0.75] \wedge \mu_{B^2}(y) = 0.5 \wedge \mu_{B^2 P}(y)$$

$$\mu_{\tilde{B}^3}(y) = [1 \wedge 0.5] \wedge \mu_{B^3}(y) = 0.5 \wedge \mu_{B^3}(y) = 0.5 \wedge \mu_M(y)$$

$$\mu_{\tilde{B}^4}(y) = [1 \wedge 0.75] \wedge \mu_{B^4}(y) = 0.75 \wedge \mu_{B^4}(y) = 0.75 \wedge \mu_U(y)$$

$$\therefore \tilde{B} = (0.5 \wedge P) \vee (0.5 \wedge M) \vee (0.75 \wedge U)$$