The Feynman-Kac formula in the Fourier representation and its applications

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The famous Feynman-Kac (FK) formula for the operator $H = -\Delta + V$ is related to an integral over trajectories of a Brownian motion generated by $-\Delta$. This formula is extremely efficient in a variety of situations, from Financial Mathematics to Quantum Mechanics. However, it does not work (at least in the usual way) when the Laplacian Δ is replaced with a function $\kappa(\Delta)$ (say, $\sqrt{-\Delta}$ or Δ^2). In this case, it is possible to propose another integral formula, emerging in the Fourier representation, related to an integral over trajectories of a jump Markov process generated by the potential term V. In this talk I will explain the Fourier-FK-formula and give examples of its application.